

# Amplitude-Modulated Rf field

```
Needs["SpinDynamica`"]
```

```
SetSpinSystem[1]
```

```
SetSpinSystem: the spin system has been set to  $\left\{\left\{1, \frac{1}{2}\right\}\right\}$ 
```

Amplitude-Modulated rf field simulated in the laboratory frame; no relaxation

this example shows the simulation of evolution under a time-dependent Hamiltonian. In this case a laboratory frame simulation is performed using an amplitude-modulated rf field

$$\omega_0 = 2 \pi 10^6$$

$$2000000 \pi$$

$$\omega_{\text{nut}} = 2 \pi 50 \times 10^3$$

$$100000 \pi$$

$$\tau_{360} = 2 \pi / \omega_{\text{nut}}$$

$$\frac{1}{50000}$$

$$\tau_{90} = \tau_{360} / 4; \quad \tau_{180} = \tau_{360} / 2;$$

the following syntax shows how to define a time-dependent Hamiltonian function, in this case a cosine modulated rf field

```
HamiltonianFunction = Function[t,  $\omega_0 \text{opI}["z"] + \omega_{\text{nut}} (2 \text{opI}["x"] \text{Cos}[\omega_0 t])$ ]
```

```
Function[t,  $\omega_0 \text{opI}[z] + \omega_{\text{nut}} (2 \text{opI}[x] \text{Cos}[\omega_0 t])$ ]
```

in this simple example, the time-dependent Hamiltonian is applied for the duration of a 180° pulse. In general, any sequence of events of various types may be defined.

```
events = {{HamiltonianFunction,  $\tau_{180}$ }}
```

```
{{Function[t,  $\omega_0 \text{opI}[z] + \omega_{\text{nut}} (2 \text{opI}[x] \text{Cos}[\omega_0 t])$ ],  $\frac{1}{100000}$ }}
```

```
{Ixtraj, Iytraj, Iztraj} =
```

```
Trajectory[opI["z"] -> {opI["x"], opI["y"], opI["z"]}, events]
```

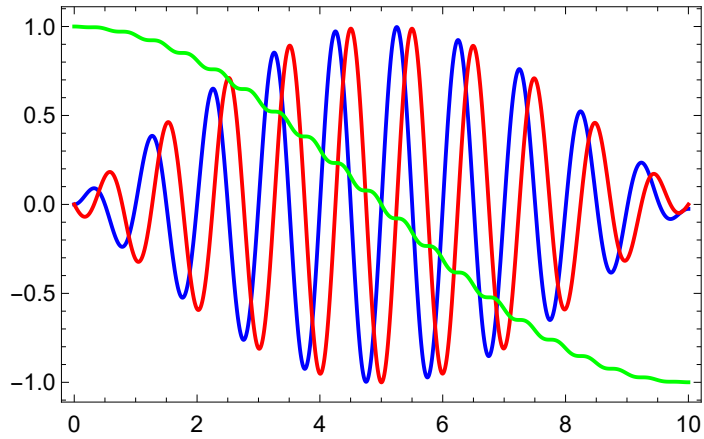
```
{TrajectoryFunction[{{0,  $10. \times 10^{-6}$ }}, <>],
```

```
TrajectoryFunction[{{0,  $10. \times 10^{-6}$ }}, <>], TrajectoryFunction[{{0,  $10. \times 10^{-6}$ }}, <>]}
```

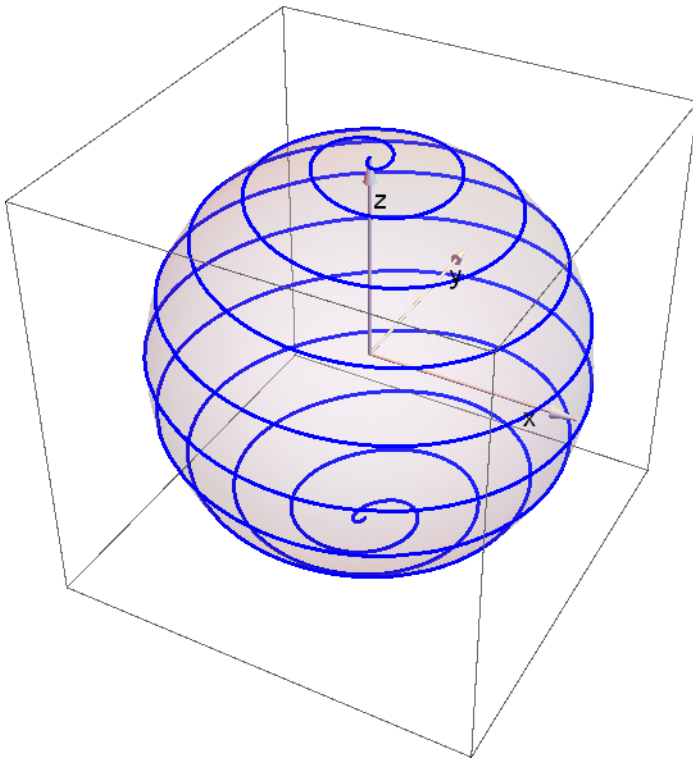
```
EventDuration[events]
```

$$\frac{1}{100000}$$

```
Plot[
  Evaluate[Through[{Ixtraj, Iytraj, Iztraj}[t $\mu$ s  $\times$  10-6]],
    {t $\mu$ s, 0, EventDuration[events]  $\times$  106},
    Frame  $\rightarrow$  True,
    PlotStyle  $\rightarrow$  {{Thick, Blue}, {Thick, Red}, {Thick, Green}},
    LabelStyle  $\rightarrow$  Directive[Medium, FontFamily  $\rightarrow$  "Helvetica"]
]
```



```
Show[
  Graphics3D@{Opacity[0.2], Sphere[{0, 0, 0}, 1]},
  ParametricPlot3D[
    Through[{Ixtraj, Iytraj, Iztraj}[t]], {t, 0, EventDuration[events]},
    Boxed  $\rightarrow$  True, Axes  $\rightarrow$  None, PlotStyle  $\rightarrow$  {{Thick, Blue}}
  ],
  Axes3D[]
]
```



Amplitude-Modulated rf field simulated in the laboratory frame; with relaxation

in this case a strong relaxation superoperator is included in the BackgroundGenerator. Evolution over 5 complete nutations is simulated.

```
 $\omega_0 = 2 \pi 10^6;$ 
```

```
 $\omega_{\text{nut}} = 2 \pi 50 \times 10^3;$ 
```

```
 $\tau_{360} = 2 \pi / \omega_{\text{nut}};$ 
```

```
 $\tau_{90} = \tau_{360} / 4; \tau_{180} = \tau_{360} / 2;$ 
```

```
HamiltonianFunction = Function[t,  $\omega_0 \text{opI}["z"] + \omega_{\text{nut}} \times (2 \text{opI}["x"] \text{Cos}[\omega_0 t])$ ]
```

```
Function[t,  $\omega_0 \text{opI}[z] + \omega_{\text{nut}} (2 \text{opI}[x] \text{Cos}[\omega_0 t])$ ]
```

the relaxation superoperator defined below corresponds to fluctuating random fields along the z-axis.

```
relaxationstrength =  $10^5;$ 
```

```
RelaxationSuperoperator =
```

```
-relaxationstrength DoubleCommutationSuperoperator[opT[1, {1, 0}], opT[1, {1, 0}]]
```

```
-100000 DoubleCommutationSuperoperator[I1z, I1z]
```

```
events = {{HamiltonianFunction, 5  $\tau_{360}$ }}
```

```
{Function[t,  $\omega_0 \text{opI}[z] + \omega_{\text{nut}} (2 \text{opI}[x] \text{Cos}[\omega_0 t])$ ],  $\frac{1}{10000}$ }
```

```
traj = Trajectory[
```

```
  opI["z"] -> opI["z"],
```

```
  events,
```

```
  BackgroundGenerator -> RelaxationSuperoperator
```

```
]
```

```
TrajectoryFunction[{{0,  $100. \times 10^{-6}$ }}, <>]
```

```
Trajectory[
```

```
  opI["z"] -> {opI["x"], opI["y"], opI["z"]},
```

```
  events,
```

```
  BackgroundGenerator -> RelaxationSuperoperator
```

```
]
```

```
{TrajectoryFunction[{{0,  $100. \times 10^{-6}$ }}, <>],
```

```
TrajectoryFunction[{{0,  $100. \times 10^{-6}$ }}, <>],
```

```
TrajectoryFunction[{{0,  $100. \times 10^{-6}$ }}, <>]}
```

```
{Ixtraj, Iytraj, Iztraj} =
```

```
Trajectory[
```

```
  opI["z"] -> {opI["x"], opI["y"], opI["z"]},
```

```
  events,
```

```
  BackgroundGenerator -> RelaxationSuperoperator
```

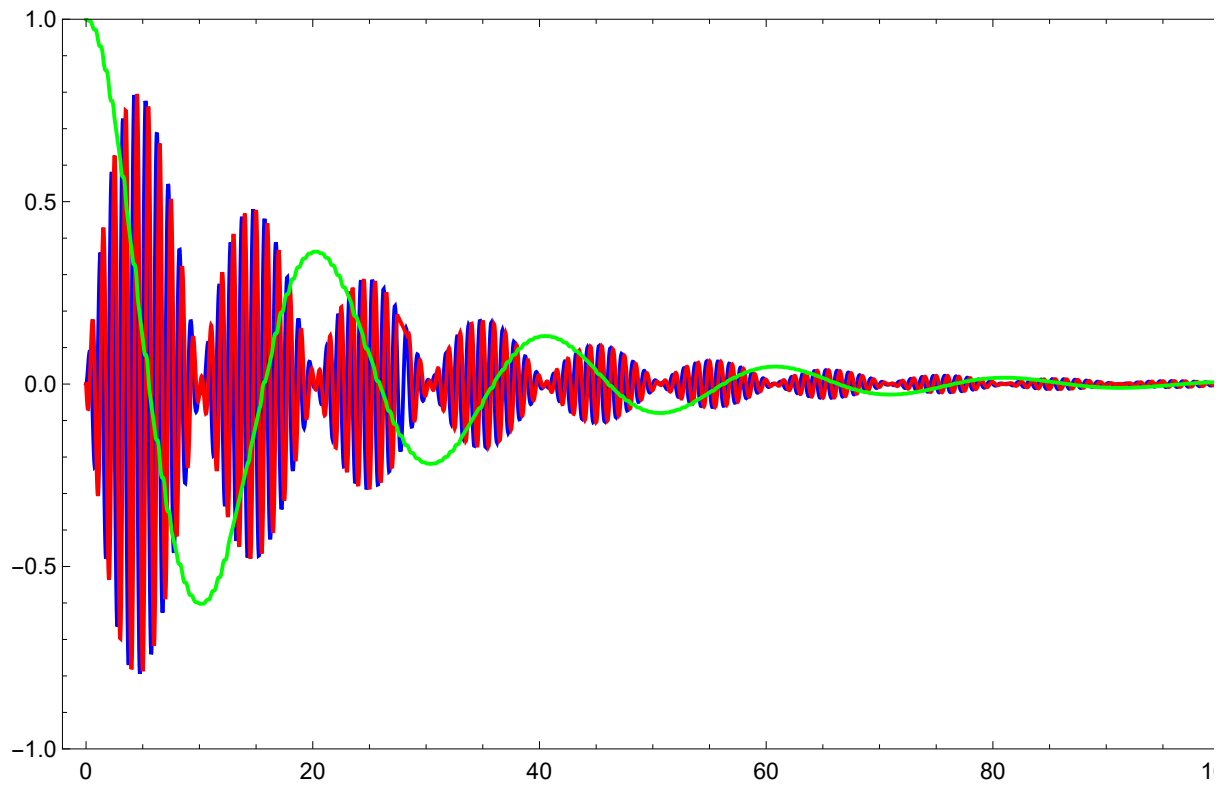
```
]
```

```
{TrajectoryFunction[{{0,  $100. \times 10^{-6}$ }}, <>],
```

```
TrajectoryFunction[{{0,  $100. \times 10^{-6}$ }}, <>],
```

```
TrajectoryFunction[{{0,  $100. \times 10^{-6}$ }}, <>]}
```

```
Plot[Evaluate[Through[{Ixtraj, Iytraj, Iztraj}[t $\mu$ s  $\times$  10-6]],  
{t $\mu$ s,  $\theta$ , EventDuration[events]  $\times$  106}, Frame  $\rightarrow$  True,  
PlotStyle  $\rightarrow$  {{Thick, Blue}, {Thick, Red}, {Thick, Green}},  
PlotRange  $\rightarrow$  {-1, 1}, LabelStyle  $\rightarrow$  Directive[Medium, FontFamily  $\rightarrow$  "Helvetica"]]
```



```
Show[
Graphics3D@{Opacity[0.2], Sphere[{0, 0, 0}, 1]},
ParametricPlot3D[
Through[{Ixtraj, Iytraj, Iztraj}[t]], {t, 0, EventDuration[events]},
Boxed → True, Axes → None, PlotStyle → {{Thick, Blue}}
],
Axes3D[]
]
```

